

Math 225 Foundations of Advanced Mathematics section 003 Spring, 2021
TuTh, 11:45 am – 1:00 pm; Online only

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Office Hours: TuTh 2.00-3.00 p.m. online or by appointment – email me!

Book: The book by Prof. Jo-Ann Cohen is online as pdf files (linked at [webpage](#))

Prerequisite: MA 241.

Homework, tests and final:

1. Weekly Homework Assignments (10% of final grade) **due Thursdays.**
2. Three in-class exams (60%): dates to be decided
3. Final Exam: (30%)

Basic Grading Scale: 90%-100%: A, 80%-89%: B, etc. (+ and – will also be used.)

Syllabus: complete syllabus and course materials can be found at the class [webpage](#)

Approximate schedule:

Chapter 0. Preliminaries: 1-2 days

Chapter 1. Language, Logic, Sets, and Methods of Proofs: 3-5 weeks

Chapter 2. The Principle of Mathematical Induction: 1-2 weeks

Chapter 3. Functions: 2-3 weeks

Chapter 4. Equivalence Relations: 2 weeks

Chapter 5. Properties of the Integers: 1-2 weeks

Chapter 6. The Size of Sets: 1-2 weeks

Summary: First few weeks: Language and notation of Mathematics; How to write proofs for number properties; Writing proofs for sets.

Then: Proofs using induction (about 1 week); Properties of functions and mappings between sets (few more weeks); Relations and equivalence relations (couple of weeks); Using these topics to describe how to measure the size of sets (finite, countable, uncountable).

Course Outline: The primary goal of Math 225 is to prepare you for upper level courses in mathematics, especially courses that rely on understanding and writing mathematics. The course includes an introduction to the format of definition, theorem and proof, the design and writing of logical arguments and formal proofs, and techniques of problem solving in higher level mathematics. During the semester, fundamental concepts in several areas of mathematics are introduced, partly to show the structure of mathematical writing in different contexts, but also to lay the foundations for higher level courses such as abstract algebra and analysis.

Student Learning Objectives/Outcomes: Students should demonstrate the ability to:

1. read, understand, and make informed judgments about mathematical arguments.
 - Students should be able to identify the basic methods of proof such as direct proofs, proofs by contradiction, and proofs using the Principle of Mathematical Induction and equivalent principles.
 - Students should be able to analyze and critique mathematical arguments. Students should be able to make a sound case as to the correctness of the argument, should be able to explain any problems that are found, and then should be able to suggest ways to remedy the problems.
2. generate clearly reasoned, convincing proofs.
 - Students should be able to construct proofs using direct arguments, contradiction, and the Principle of Mathematical Induction and equivalent principles.

- Students should be able to move successfully from the discovery of a proof to the writing of a proof.
 - Students should be able to construct a proof in such a way that the reader can follow the steps logically from one to another and is convinced of the validity of the proof.
 - Students should be able to show that they possess a sound understanding of the underlying mathematics as revealed in the construction of proofs.
3. clearly communicate mathematics (in both written form and oral form) at the appropriate levels for the audience.
 4. understand and use mathematical language and symbols.
 - Students should be able to express mathematical concepts using precise mathematical symbols and prose.
 5. explore examples and make conjectures.
 6. understand the basic definitions and properties of selected mathematical concepts beyond calculus and high school material.
 - Students should be able to use these definitions and properties in the construction of proofs.

Course Delivery Changes Related to COVID-19: Please be aware that the situation regarding COVID-19 is frequently changing, and the delivery mode of this course may need to change accordingly, including possibly moving from synchronous sessions to an asynchronous format. Regardless of the delivery method, we will all strive to provide a high-quality learning experience.

Note: If I need to be out for an extended period of time, Dr. Patrick Sprenger will take over in my absence.

Wellness Days: The wellness days for Spring 2021 are: Tuesday, February 9th, Friday, March 5th, Wednesday, March 24th, and Thursday, April 15th. We will not have class on those days and will not have tests or assignments due on any of those days.

Email: All emails will be sent to your official ncsu.edu email address.

Additional Policies:

1. *I encourage you to discuss homework with other students, or with me during office hours.* You should be aware that the homework is intended for you to learn from the course; working on homework at least in part on your own will help you master the material, keep up with the course and prepare for tests. Homework will be graded on a scale of 1-10. Points will be awarded for amount of homework attempted; selected problems will be graded in detail. Please hand in assignments carefully written; illegible or sloppy homework will not be graded.
2. *I expect you to read sections of the book around the time of lectures.* Homework assignments will typically be from those sections. The book has additional examples and discussion that you will find helpful. Some test questions may resemble examples from the book.
3. *You are expected to attend all classes on time.* Classroom discussion and questions in class help clarify issues in this course, so please feel free to participate by asking questions. Late assignments and make-up work will only be allowed for excused absences. You should contact me by email before any anticipated excused absence. If you have an unanticipated excused absence (for example, a medical emergency), you should contact me within one week of returning to class. For complete attendance and excused absence policies, please see: <https://policies.ncsu.edu/regulation/reg-02-20-03-attendance-regulations/>.
4. If you are unavoidably absent from a test, a score for that test will be assessed at the end of the semester, based on your performance in homework, the other tests, and on the final, with an emphasis on the material of the missed test. Attendance regulations can be found at <http://policies.ncsu.edu/regulation/reg-02-20-03>

Academic Integrity Statement: Students are expected to follow university policies on academic integrity and the Honor Pledge, which may be viewed by following the links at: <http://policies.ncsu.edu/policy/pol-11-35-01>

Grading/Scheduling Changing Options Related to COVID-19: If the delivery mode has a negative impact on your academic performance in this course, the university has provided tools to potentially reduce the impact:

Enhanced S/U Grading Option: [Enhanced Satisfactory/ Unsatisfactory Grading Option](#)

Late Drop: [Enhanced Late Drop Option](#)

Be aware that if you use the enhanced S/U grading option, you will need to complete the course and receive at least a C- to pass the course.

In some cases, another option may be to request an incomplete in the course. Before using any of these tools, please discuss the options with me and with your academic advisor.

Auditing the Course: To audit the course, you must have the approval of your advisor and the Mathematics Department. In order to receive an AU, you must attend the majority of the sessions, and you must hand in all of the homework and take all of the tests. See:

<https://policies.ncsu.edu/regulation/reg-02-20-04/> for more information concerning course audits.

Incomplete Grades: Incomplete grades will be handled on an individual basis. Note, however, that if an extended deadline is not authorized by an instructor or department, an unfinished incomplete grade will automatically change to an F after either (a) the end of the next regular semester in which the student is enrolled (not including summer sessions), or (b) the end of 12 months if the student is not enrolled, whichever is shorter. Incompletes that change to F will count as attempted courses on transcripts. The burden of fulfilling an incomplete grade is the responsibility of the student. The university policy on incomplete grades is located at: <https://policies.ncsu.edu/regulation/reg-02-50-03/>.

COVID-19 Related Absences: If you need to miss class because you have been advised that you may have been exposed to COVID-19 or you have a personal or family situation related to COVID-19 that prevents you from attending our sessions, please contact me. Together we will develop a plan to help you keep up with your coursework during any such absences. COVID 19-related absences will be considered excused. You do not need any additional documentation. (But, again, please make sure you contact me.)

Academic Integrity/Honesty: Students are required to comply with the university policy on academic integrity/honesty found in the Code of Student Conduct: <https://policies.ncsu.edu/policy/pol-11-35-01/>. Your signature on any test or assignment means that you have adhered to the Pack Pledge:

I have neither given nor received unauthorized aid on this test or assignment.

Violations of academic integrity will be handled in accordance with the Student Discipline Procedures ([NCSU REG 11.35.02](#)).

Digital Course Components: In this course we will use Zoom and Moodle. Please see the relevant [technology requirements](#). If you need access to additional technological support, please contact the Libraries' Technology Lending Service ([Technology Lending](#)).

Students may be required to disclose personally identifiable information to other students in the course, via electronic tools like email or web-postings, where relevant to the course. Examples include online

discussions of class topics and posting of student coursework. All students are expected to respect the privacy of each other by not sharing or using such information outside the course.

Moodle: All reading materials are housed on the course website. Throughout the semester you will need to upload homework and tests in Moodle as pdfs. So make sure you have an app that will allow you to scan your work if you are not able to directly save your work as a pdf.

Zoom: Our “lectures” will be conducted synchronously via Zoom **TuTh, 11:45 am – 1:00 pm**. I will initially put all of you on "mute", but if you want to talk, there is a button on the left side of the Zoom screen that will enable you to unmute yourself. Zoom enables us to have breakout rooms for small group discussions and we will utilize that function as well.

I will be recording our Zoom sessions and will be posting links to the recordings on our Moodle page for your use. I will only record our mathematical discussions and not, for example, the parts of our sessions where we check in with each other. In order that all students in the class feel comfortable asking questions, and making conjectures, etc., you may not share the links to the recordings with anyone outside of our class.

These recordings are for use in our current class (and possibly for use in future educational activities). By your continued participation in this recorded course, you are providing your permission to be recorded for use in our class and for use in future educational activities.

Diversity, Equity, and Inclusion: Diversity, equity, and inclusion are important to the success of our students at NC State. Every student, every faculty member, and every staff member who comes to NC State enriches us through their varied perspectives, knowledge, and backgrounds. Our classroom is one in which every student is respected and feels heard. If you wish to share your experiences with me, be assured I will listen, give advice as appropriate, and I will advocate for you to a higher level if you wish to take any complaint, for example over discrimination or harassment. See the non-discrimination policy below.

In an effort to affirm and respect the identities of transgender students in the classroom and beyond, please contact me if you wish to be referred to using a name and/or pronouns other than those listed in the student directory.

I welcome any additional suggestions you have for making our classroom more welcoming and inclusive.

Accommodations for Disabilities: Reasonable accommodations will be made for students with verifiable disabilities. In order to take advantage of available accommodations, students must register with the Disability Resource Office at Holmes Hall, Suite 304, 2751 Cates Avenue, Campus Box 7509, 919-515-7653. For more information on NC State’s policy on working with students with disabilities, please see the [Academic Accommodations for Students with Disabilities Regulation \(REG02.20.01\)](#).

Non-Discrimination Policy: NC State prohibits discrimination, harassment, and retaliation based on a person’s age (40 years or older), color, disability, genetic information, gender identity, national origin, race, religion, sex (including pregnancy), sexual orientation or veteran status. If you feel that you have been the subject of prohibited discrimination, harassment, or retaliation, you should contact the Office for Institutional Equity and Diversity (OIED) at 919-513-0574.

NC State's policies and regulations covering discrimination, harassment, and retaliation may be accessed at <http://policies.ncsu.edu/policy/pol-04-25-05> or <http://oied.ncsu.edu/divweb>.

Health and Well-Being Resources: These are difficult times, and academic and personal stress are natural results. Everyone is encouraged to [take care of themselves](#) and their peers. If you need additional support, there are many resources on campus to help you:

- Counseling Center ([NCSU Counseling Center](#))
- Health Center ([Health Services | Student](#))
- NC State CARES Team: As members of the NC State Wolfpack community, we each share a personal responsibility to express concern for one another and to ensure that our campus remains a healthy and safe environment for learning. Occasionally, you may come across a classmate whose personal behavior concerns or worries you, either for your classmate's well-being, for your well-being, or for the well-being of others. When this is the case, I would encourage you to report the behavior to the NC State CARES team: ([Share a Concern](#)).
- If you or someone you know are experiencing food, housing or financial insecurity, please see the Pack Essentials Program ([Pack Essentials](#)).

Additional COVID-19 Information: Due to the Coronavirus pandemic, public health measures have been implemented across campus. Students should stay current with these practices and expectations through the [Protect the Pack](#) website (<https://www.ncsu.edu/coronavirus/>.)

We are most concerned about your health and the health of the students, faculty, and staff across campus. If you test positive for COVID-19, or are told by a healthcare provider that you are presumed positive for the virus, please follow university guidelines, including self-reporting ([Coronavirus Self Reporting](#)): Self-reporting is not only to help provide support to you, but also to assist in contact tracing for containing the spread of the virus.

Community Standards related to COVID-19: We are all responsible for protecting ourselves and our community. Please see the [Community Standards](#) and Rule 04.21.01 regarding Personal Safety Requirements Related to COVID-19 ([RUL 04.21.01 – Personal Safety Requirements Related to COVID-19 – Policies, Regulations & Rules](#)).

NC State Rules and Regulations: Students are responsible for reviewing the NC State University Policies, Rules, and Regulations (PRRs) which pertain to their course rights and responsibilities, including those referenced both below and above in this syllabus:

- Equal Opportunity and Non-Discrimination Policy Statement <https://policies.ncsu.edu/policy/pol-04-25-05/> with additional references at <https://oied.ncsu.edu/equity/policies/>
- Code of Student Conduct <https://policies.ncsu.edu/policy/pol-11-35-01/>

Important Resources for Students

- **NC State Keep Learning, tips for students taking courses remotely:** <https://dasa.ncsu.edu/academics/keep-learning/>
- **Introduction to Zoom for Students:** <https://youtu.be/5LbPzzPbYEw>
- **Learning with Moodle, a student's guide to using Moodle:** <https://moodle-projects.wolfware.ncsu.edu/course/view.php?id=226>
- **Protect the Pack FAQs:** <https://www.ncsu.edu/coronavirus/frequently-asked-questions/>

- **NC State Protect the Pack Resources for Students:**
<https://www.ncsu.edu/coronavirus/reactivating-campus/resources-for-students/>